

- (a) Let  $a < b$ ,  $c > 0$ ,  $f$  a function that is integrable on  $[ca, cb]$ . Use the definition of integral to prove that  $\int_{ca}^{cb} f(x) dx = c \int_a^b f(cx) dx$ . *Hint:* a partition  $x_0 < x_1 < \cdots < x_n$  of  $[a, b]$  induces a partition  $cx_0 < cx_1 < \cdots < cx_n$  of  $[ca, cb]$  and conversely.
- (b) Assuming that a disk of radius 1 has area  $\pi$ , prove that the area enclosed by the ellipse  $x^2/a^2 + y^2/b^2 = 1$  is  $\pi ab$ .